

# **Lecture 16: Contracting, or The Rules of the Game**

**(See McMillan, Chapters 8, 9)**

## **Topics:**

- 1. Strategising versus Economising**
- 2. Using Game Theory to Enhance Efficiency**
- 3. Creating Incentives**
- 4. Designing Contracts**
- 5. Application to Financial Contracts**

# I. Strategising versus Economising

## *Strategising ...*

**(See Williamson's paper in the Package)**

**Game Theory is usually applied to issues of “*strategising*”, i.e., beating rivals or consumers:**

- **Pre-emptive threats/entry deterrence.**
- **Cartel enforcement.**
- **Bargaining and bidding.**

## **... versus Economising**

***Economising* – the positive-sum, efficiency-enhancing aspects – often neglected in game theory (and in corporate strategy).**

**Why is it neglected?**

**There are two illusions:**

- 1. Illusion from micro theory that it's easy to minimise costs: set Wage = Value of the Marginal Product of Labour.**

**But this is very difficult and costly to monitor on the shop floor.**

- 2. Illusion that powerful tools from game theory don't help to economise, in Finance or in Human Resource Management.**

**But game theory can be very useful, especially for economising.**

## Contracts Integrate ...

**Contracts integrate game theory and standard microeconomics:**

- ***A contract:*** an agreement that supports exchange between supplier (seller) and buyer (demander).
- **Standard microeconomics:** Supply = Demand (and produce where Marginal Cost = Price) is just the Nash equilibrium of a game where no-one's decisions affect the welfare of anyone else. (Perfect competition, and all are price-takers.)
- **Costless contracts:** Even with small numbers, can achieve the perfect competition outcome.

## Prediction and Design

**Game Theory helps in a real world of costly contracts — twice:**

- 1. Predicts (or analyses) what will happen under different contractual arrangements.**

**What are the *incentives*?**

- 2. Allows us to choose (or to design) the *best* one, (Choosing the Game).**

**e.g.:**

- Make or Buy? (production integration)**
- Debt or Equity? (capital structure)**
- Privatised or Publicly Owned? (ownership)**
- Division or Spin Off? (organisational structure)**

## 2. Using Game Theory to Enhance Efficiency

### General Principles

1. **Game theory is often taught via simple examples, chosen on an ad-hoc basis. e.g. battles, interactions, kids and credibility.**
2. **The Contracting perspective, by contrast, is:**
  - ***choose* the game, the contract,**
  - **solve (or simulate) for the equilibrium of the game, the contract,**
  - ***then* ask:**
    - **are the players *pleased* with the outcomes?**
    - **what could they do to achieve a *better* outcome? How?**

## Choosing the rules of engagement

- 3. Basic idea: when you negotiate a contract with someone, you are proposing to play a game, structured by the contract.**

**Since you must get them to play, *and* they solve for the equilibrium as you do, it *pays you to choose the game (the contract) with the most efficient outcome*, to maximise the size of the pie, given a claim over fixed % slice.**

**e.g. employment contract — pay, conditions, work, supervisor's interests, etc;**

**e.g. financing contract**

**e.g. franchise contract**

**e.g. outsourcing contract**

### 3. Creating Incentives

**Q: How can you make it in another person's interest to behave as you want? Especially with a divergence of interests, aims.**

**Q: How can you create appropriate *incentives*?**

**A: Rewards & punishments – carrots & sticks.**

➤ **The pervasive *Principal–Agent* problems:**

- author v. publisher
- debt v. equity
- landlord v. tenant
- subcontractor v. price contractor
- employer v. employee
- insured v. insurer

➤ **Whereas HRM: change the agent's goals → the principal's goals, now on the contrary ...**

➤ **Here: we focus on the use of monetary rewards – important (although not necessary) and simple to understand.**

## **Piece Rates, Commissions, & Royalties**

**Performance incentives are ubiquitous —**

- piece rates/bonuses/commissions for production workers**
- pay for performance (bonuses, share options)**
- sales representatives paid by commission**
- professional sports? (tournaments, winner-takes-most)**
- academic salary supplements**
- forecasters' pay  $\propto$  accuracy (?)**

**Contracts can also be used in *cost minimisation* instead of maximum output:**

- **cost-minimisation is costly**
- **contracts vary from one extreme to another – who bears the risk?**
  - **fixed-price contracts?**
  - **cost-plus contracts?**
  - **incentive contracts?**

***A verbal contract isn't worth the paper it's written on.***

**– Samuel Goldwyn**

## Marginal Incentives

**If the principal can cheaply, perfectly, monitor the agent's "effort":**

**then no problem:**

**→ simply link payments to effort.**

**But usually impossible or costly to monitor the agent's effort, so**

- link pay to *performance*, not *effort*, or link pay to *output*, not *input***
- OK if constant, predictable relationship: effort  $\Rightarrow$  performance**
- but random events, uncertainties intervene i.e. the agent may be unlucky or lucky.**
- the agent may "slack" or "shirk"**

## **Principals' and agents' interests may diverge.**

- So:**
- 1. Divergence of interests.**
  - 2. Imperfectly observable “efforts” of the agent.**
    - not necessarily how hard the agent works**
    - but to what end does the agent toil? (profits, or size, etc.?)**

**The incentive effort – is at the *margin*,  
where costs of extra effort = gain to the agent  
from extra effort.**

**The higher the commission rate  $\lambda$ , then the greater the selling effort.**

## Carrots & Sticks

**Look at from the worker's point of view:**

- **if she performs better, do her pay or rewards increase?**
- **if she performs worse, does her pay fall or her punishment increase?**

**Ideally we'd like:**

- **Piece rates or commission as a continuum:**

$$\frac{\Delta \text{reward}}{\Delta \text{performance}} > 0$$

**where performance is measurable.**

## But incentive schemes can distort behaviour.

➤ They are often discontinuous:

$$\frac{\Delta \text{ reward}}{\Delta \text{ performance}} = 0 \text{ or } \frac{\Delta \text{ punishment}}{\Delta \text{ performance}} = 0$$

- threat of firing, loss of contract
- fines
- legal liabilities
- prizes, promotions, bonuses

➤ But discontinuous incentive schemes can substitute for continuous:

- wage (\$/hr) + punishment after monitoring (firing)
- wage (\$/hr) + reward after monitoring (promotion)

## Multi-Dimensional Performance

### A danger:

- not that incentive schemes fail, but
- but that they work too well.

**Agents concentrate on the goal with explicit incentives, often quantity (easy to count).**

### One tradeoff: *Quality*

- quantity v. quality  
e.g. jet engine blades  
e.g. production-line workers,  
“shirking” = higher defect rates
- when quality is hard to monitor  
e.g. solution: pay all but the quality-control workers by the piece, since it is difficult to control the quality of quality control (-:-)

## **Moral hazard might be suspected**

- **even with time payment, we can use discontinuous rewards/punishments to mimic continuous incentive schemes.**

**e.g. Sears ended its commission to its mechanics, to enhance its credibility with its customers, who suspected over-servicing as a result of the mechanics' incentives.**

## The Principal's Ideal Payment Scheme

**“The shortest and best way to make your fortune is to let people see clearly that it is in their interests to promote yours.”**

**— Jean de La Bruyère (1645–1696)**

**Q: But how?**

**A: Set the agent's marginal payment scheme  $\lambda$  (commission, royalty, piece rate, etc.) at 100%.**

## Example: the salesperson example:

**Q: What is the ideal amount of the agent's effort, from the principal's viewpoint?**

– Assume the agent's costs equal the principal's; and assume diminishing return to effort.

– If the principal acts alone: gets 100% of the benefits and incurs 100% of the costs.

So exerts effort to the point where marginal costs equal marginal returns

or effort: marginal cost (effort) = marginal returns  
( $P = MC?$ )

– When the agent acts, he bears the full cost of any marginal effort, whatever the commission rate  $\lambda$ .

## Optimal commission? How to raise money?

- **At  $\lambda = 30\%$ , the agent would exert effort up to the point where the cost of \$100 extra sales is \$30, which is less than the principal's effort (of \$100).**
  - **With  $\lambda = 100\%$ , the agent reaps the full benefits, and exerts effort up to the point where the cost of \$100 extra sales is \$100, as does the principal.**
  - **Thus  $\lambda = 100\% \Rightarrow$  the agent's interests and the principal's are identical, and the gain from trade to be divided between the principal and the agent is maximised.**
- Q: But then how does the principal earn anything from the deal?**

## How about a fixed payment by the agent as well?

- As well as the commission rate  $\lambda$ , the deal includes a fixed payment  $f$  from  $A$  to  $P$ .
  - The principal uses the rate  $\lambda$  to induce appropriate actions by the agent at the margin, and the fixed fee  $f$  to get some of the gains to trade for herself. (Limited by the agent's alternatives, given the agent's veto.)
  - The fixed fee  $f$  is a payment from the agent to the principal.
- ∴ In effect the principal sells the agent the right to be the agent:  
self-employed, arm's-length relationship.

e.g. Lord Cornwallis in Bengal, in the late eighteenth century.

## 4. Designing Contracts

**Ideal contracts (100% marginal payment schemes) are seldom seen.**

**Two flaws:**

**Contracts do more than generate incentives for effort:**

- 1. (asymmetric information): if the principal can't know how productive the agent is, then she may want to offer a "menu" of contracts to induce the agent to reveal his productivity – private information; *screening*, *sorting*.**
- 2. the agent's performance is a function of outside events, but the agent bears all of the risk – but if the agent is *risk averse*, it may not be in the principal's interest to force the agent to bear the risk.**

## **Contracting with Private Information**

**e.g. The sales manager (the principal) knows only that the value of a particular area is either high or low, but only the salesperson (the agent) knows which.**

**Possible for the manager to offer the agent a different package (commission rate  $\lambda$  and base salary  $B$ ) depending on whether the agent reports his sales potential as high or low, subject to the agent's fallback position.**

**Accountability for what they report?**

## Honesty?

**Possible (with appropriate packages – see McMillan Ch. 9) to induce the agent to give an honest report:**

- **Total package payments must be higher when the potential is correctly reported as high than when correctly reported as low.**
- **Commission rate  $\lambda$  must be higher, and the base salary  $B$  lower, for a report of high potential than for a report of low potential.**

## How well does the principal do?

**The commission rate  $\lambda$  must do double duty:**

- 1. elicit information, and**
  - 2. elicit effort (as above)**
- $\therefore$  it must be less than 100%,**
- $\therefore$  the agent's private information costs the principal.**

**Useful to use salespeople's information in contracts and in corporate planning.**

## Differential wages

**500 U.S. firms in footwear and clothing (after controlling for sex, union status, etc.): Why did piece-rate workers earn 14% more than workers on fixed wages? Three possibilities:**

- 1. self-selection: more skillful workers choose companies with piece-rate payments, while others prefer fixed salaries;**
- 2. people work harder when rewarded for the results of their extra effort;**
- 3. since piece-rate workers' pay is not only higher but more volatile than fixed-wage workers' pay, to some extent the higher earnings are compensation for *higher risk* borne by the piece-rate workers.**

## Risk-Sharing versus Incentives

**Performance-based contracts subject the agents to risk.**

**Most people are *risk-averse*: insure against risk by forgoing some of their anticipated earnings.**

**The agent is often more risk averse than the principal: a firm is better able to bear risks than its individual employees are.**

**∴ We might expect a smaller average payment to the agent in return for the principal absorbing some of the risk.**

**But this will weaken the agent's incentives:**

***NB: Any contract will be a compromise between risk-bearing and incentives.***

## **What is the principal's best tradeoff between “risk-bearing” and “incentives”?**

### **Two questions:**

- 1. How much discretionary scope does the agent have to produce variations in performance?**
- 2. How much money would the agent be prepared to forgo to have the risk associated with the task removed from his shoulders?**

**The commission rate  $\lambda$  should depend on the relative size of these two numbers.**

**So long as the principal is less risk-averse than the agent, sharing risk is a win-win proposition.**

## **Risk-Sharing via Contracts**

***A fixed-price contract* will give the agent – the firm or person contracting with the firm or government (the principal) – the incentive to choose the effort level that maximises the total return from the transaction, but at risk.**

***A cost-plus contract* puts the risk on the principal, but has the disadvantage of giving the agent no incentive to limit production costs.**

***An incentive contract* is an intermediate form: allows the agent to pass on some fraction of added cost as higher price to the principal.**

## Relative Performance Evaluation

**With perfect information, in order to infer the agent's actions, the principal could design a contract to elicit the desired actions.**

**The principal can obtain more information than just the agent's output: the outputs of others.**

**This can be obtained through *benchmarking* with other firms, or through tournaments among agents, with prizes and rewards.**

**(See McMillan Ch. 10 on Setting Executives' Incentives.)**

## 5. Application to Financial Contracts (e.g. Hollywood)

**Or: Why standard finance theory doesn't tell you much about choice of contract.**

### I. Fundamentals:

- **A project costs \$1 million to start.**
- **It pays:**  $\left\{ \begin{array}{l} \$10 \text{ million with probability} = 3/4 \\ \$0 \text{ with probability} = 1/4 \end{array} \right.$
- **Investors are risk-neutral; and the market interest rate is 0% p.a.**

**Hence, expected NPV =  $\$10 \times 3/4 + 0 \times 1/4 - \$1$   
= \$6.5 mn > 0.**

## Finance theory and contracts.

### 2. Two common ways to raise capital: Equity, Debt.

#### ➤ *Equity contracts:*

The principal promises a share  $\lambda$  of returns ( $0 \leq \lambda \leq 1$ ) to investors.

To raise \$1 million, promise  $\lambda$  to solve:

$$\lambda [10 \times \frac{3}{4} + 0 \times \frac{1}{4}] \geq 1,$$

which  $\Rightarrow \lambda \geq 0.133 = 13.3\%$  (because their Expected Net Return  $\geq 0$ )

The principal gets  $(1 - \lambda) \times \frac{3}{4} \times 10 \leq \$6.5$  mn, the net wealth created.

## ... and Debt Contracts

- **Debt:** Promise to pay first  $\$D$  dollars to investors if a Success. Solving:

$$D \times \frac{3}{4} = 1, \Rightarrow D = \$1.33 \text{ million}$$

The principal gets  $(10 - 1.33) \times \frac{3}{4} = \$6.5$  million

- **Financing choice (debt or equity) is irrelevant (Modigliani-Miller).**

But if bankruptcy has cost  $b$ , then stay away from debt, as it gives Entrepreneur an expected value of  $6.5 - \frac{b}{4}$ , where the probability of bankruptcy is  $\frac{1}{4}$ .

**Q: So why are most projects like this (large inside ownership) financed with debt?**

## The Simplest Answer (with asymmetric info, such as Hollywood and little investors):

Cannot contract directly on realised returns, since only the *insider* knows whether the project succeeded or failed (or how successful the project was). Now compare the two securities:

### 5.1 Equity finance:

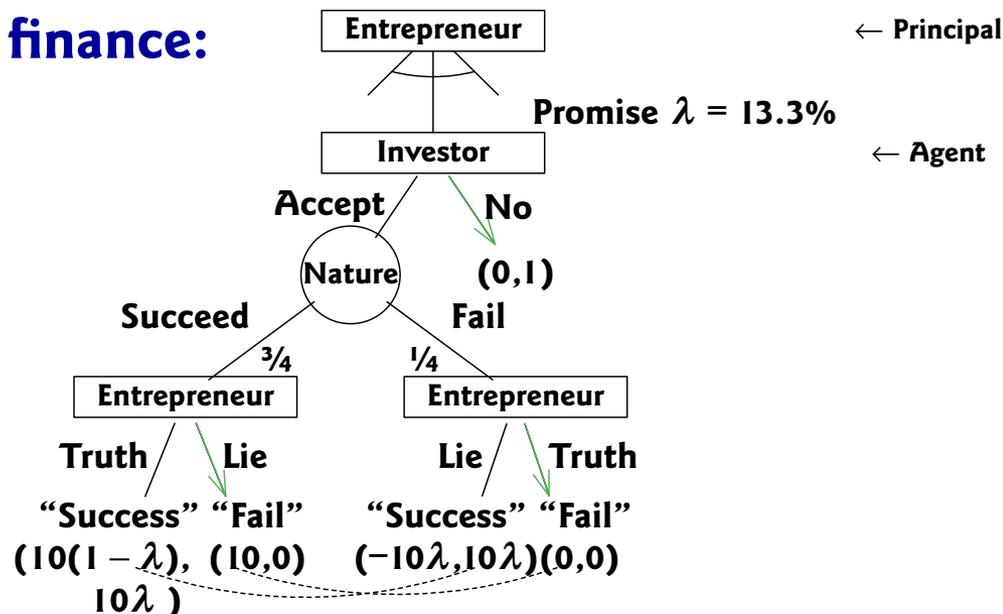


Fig 1: Equity Finance (Entrepreneur, Investor)

## **No investment – Inefficient outcome**

**The outside Investor's information set: he knows what the Entrepreneur says, but not Nature's outcome (whether there has been success or not).**

- ∴ The Entrepreneur announces “Failure” in *both* cases:  $10 > 10(1-\lambda)$  (Probability 1)**
- ∴ The Investor says No, no investment: because  $1 > 0$**
- Mutual tragedy – inefficient.**

## 5.2 Debt Finance with bankruptcy penalty $b$ (a dead-weight loss).

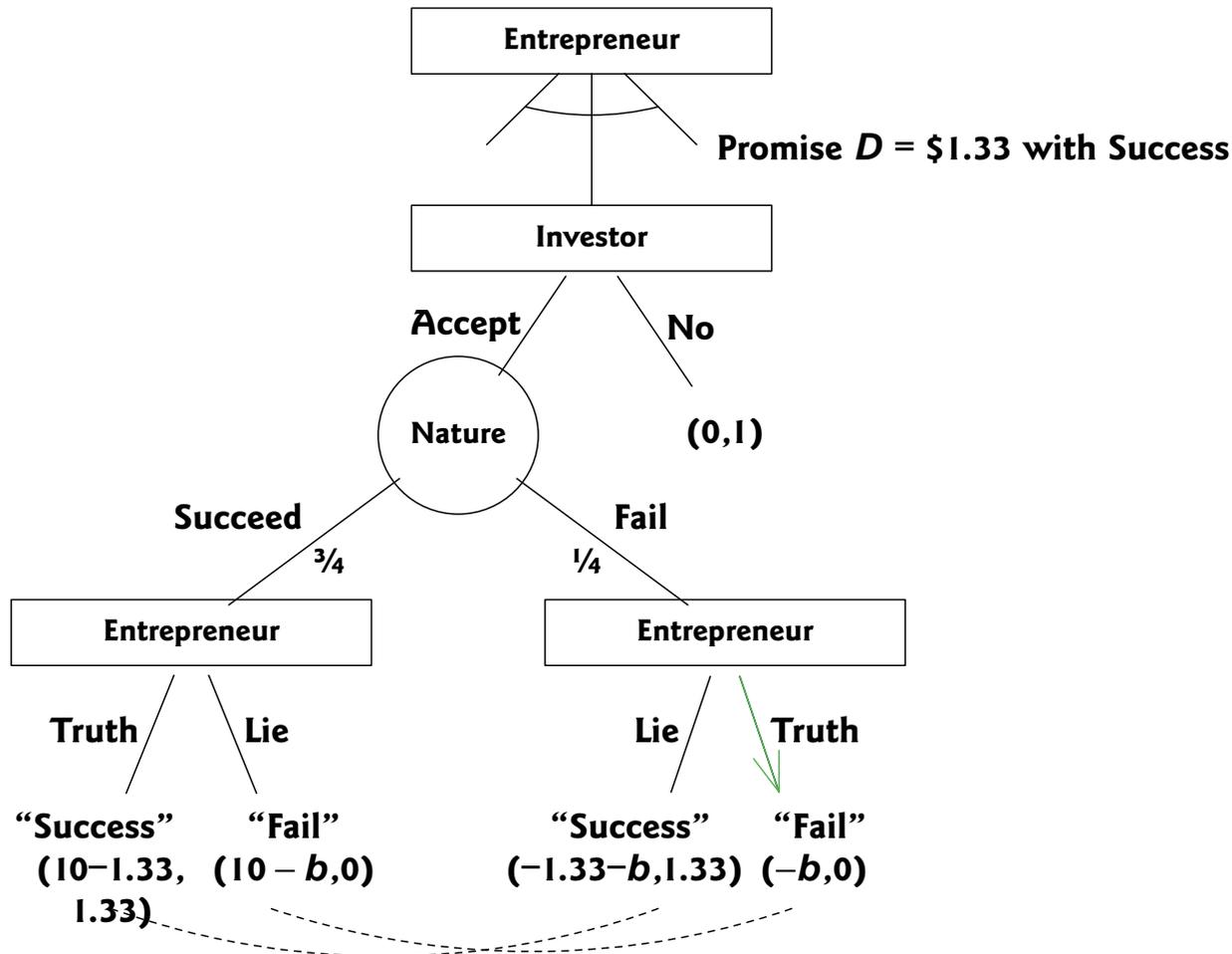


Fig 2: Debt Finance (Entrepreneur, Investor)

## The cost of bankruptcy can induce honesty:

- **The Entrepreneur tells the Truth with Success if  $b \geq \$1.33$  mn**  
(In the real world, the necessary  $b$  is scaled down by other forces, e.g., honesty, etc.)
- **The Investor then *participates*: Accept.**  
**Is this efficient?**
- **The penalty  $b$  must be invoked when failure occurs or when Entrepreneur announces “Failure”.**

**Small companies (which can hide \$ flows) can issue these contracts.**

**Q: ways to achieve at lower cost to Ent. than  $\frac{b}{4}$ ?**

**More efficient, because dead-weight loss  $b$ .**

**Intermediaries?**

**Large banks less often?**

### 5.3 “Relationship Investing” (Equity plus Monitoring)

By spending  $X$  mn dollars, the equity investor finds out whether success or failure by monitoring.

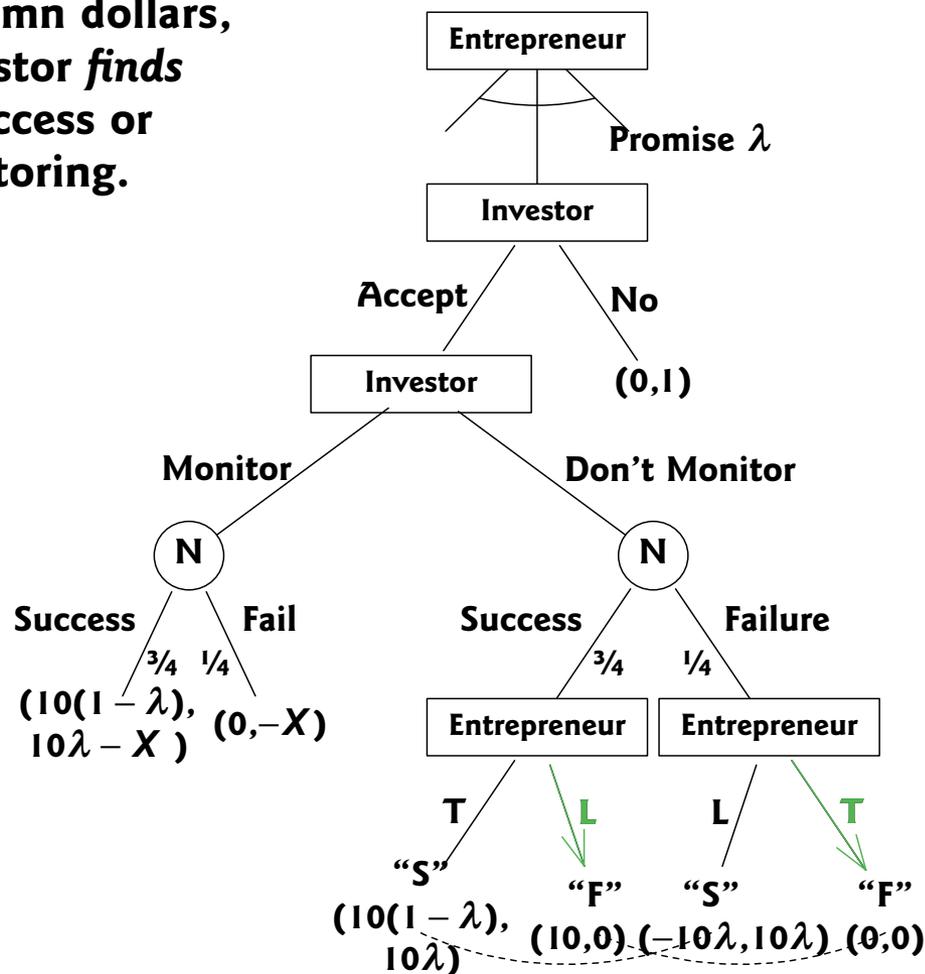


Fig 3: Relationship Investing (Entrepreneur, Investor)

## When will monitoring and investment occur?

- From Fig 3 we see that Investors know that:
  - if they don't monitor, they get 0 *for certain*, but
  - if they do monitor, then they get

$$\frac{3}{4} (10\lambda - X) + \frac{1}{4} (-X) = 7.5\lambda - X.$$

- Thus they monitor after investing, if  $7.5\lambda - X > 0$ , i.e., if  $X < 7.5\lambda$  million dollars.

- But they'll only Accept the contract if

$$7.5\lambda - X \geq 1,$$

so we must have  $\lambda \geq 0.133 + \frac{X}{7.5}$ ,

where the second term is the compensation for monitoring expense.

## 5.4 Conclusion: Debt or Relationship?

Consider the return to the Entrepreneur in Fig 2. (with  $b = \$1.33$  mn to induce truth-telling) and in Fig 3:

then choose Relationship Investing over Debt Finance if the expected return to you the Entrepreneur is higher for Relationship Investing than for Debt Finance, i.e., if:

$$7.5(1 - \lambda) > \frac{3}{4}(10 - 1.33) - \frac{b}{4},$$

where  $\frac{b}{4} = \frac{1.33}{4}$  is the dead-weight loss associated with

Debt Financing, and where  $\lambda = 0.133 + \frac{X}{7.5}$ ,

i.e., if the monitoring cost  $X < \$0.33$  mn, then choose Relationship Investment (Fig 3).

Idea: to have sunk monitoring cost before knowing the outcome, then it's redundant if you find out it's successful.

But don't have to do messy ex-post bankruptcy.