2. Basic Concepts In Project Appraisal

[DoF Ch. 4; FP Ch. 3, 4, 5]

- 1. Which Investment Criterion?
- 2. Investment Decision Criteria
- 3. Net Present Value Annual User Charge / Value On Completion / Annual Value / Annuities
- 4. Internal Rate of Return
- 5. B/C Ratio
- 6. Payback Period
- 7. Inflation
- 8. Income Tax
- 9. Discount Rates for Public- and Private-Sector Projects.
- 10. Consistency of Horizon/Residual Value
- 11. Non-Exclusive Projects
- 12. Capital Rationing

2.1 Which Investment Criterion?

[L 2.3]

Net Present Value:

$$NPV = \sum_{t=0}^{T} \frac{b(t) - c(t)}{(1+r)^t} - K,$$

where NPV = net present value from project

b(t) = benefits (\$) received from project in year t

c(t) = costs (\$) of project in year t

 $\frac{1}{1+r(t)}$ = discount factor at interest rate r p.a.

T = lifetime of project

K = initial (capital) outlay at t = 0

Questions:

(These issues will take several lectures.)

- 1. Which benefits *b* and costs *c* to include?
- 2. How are they to be valued? (i.e. shadow prices?)
- 3. At which rate(s) *r* to discount?
- 4. Which investment criterion to use?

2.2 Investment Decision Criteria

[DoF Ch. 4, App. III; FP Ch. 5]

1. Annual User Charge	(2.3)
2. Net Present Value (NPV).	(2.4)
3. Value on Completion.	(2.4.1)
4. Annuity Values	(2.4.2-3)
5. Internal Rate of Return (IRR).	(2.5)
6. Benefit/Cost Ratio (B/C).	(2.6)
7. Payback Period	(2.7)

The basis for decisons must be *opportunity cost*, or the value of options forgone. Neither IRR nor B/C can be adequately used to choose between two mutually exclusive projects.

In general, we want to compare two (or more) projects and choose one (mutually exclusive).

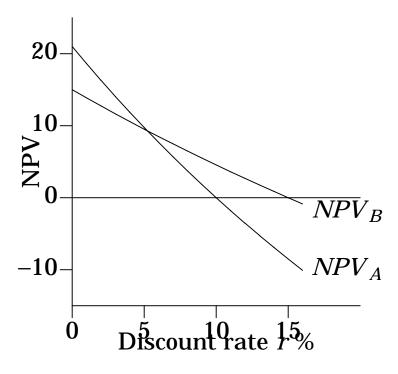
Consider two projects, A and B.

Each costs \$100 in year 0. Project A returns nothing in year 1, and \$121 in year 2. Project B returns \$115 in year 1, and nothing thereafter.

	Year 0	Year 1	Year 2
Project A	-\$100	0	\$121
Project B	-\$100	\$115	0

- At a zero discount rate, Project A is more attractive. Why?
- At a discount rate of 5.2% pa the two projects are equally attractive (and have a positive NPV).
- At a discount rate of 10% pa Project A has an NPV of zero: its IRR is 10% pa. At a discount rate of 10% pa Project B has a positive NPV.
- At a discount rate of 15% pa Project B has an NPV of zero: its IRR is 15% pa. At a discount rate of 15% pa Project A has a negative NPV.

So, choose Project A if the market rate is less than 5.2%, or Project B otherwise, if the criterion is maximizing the NPV. Choose Project B if the criterion is maximizing IRR.



Find r_1 where two projects have equal NPV by solving for r_1 :

$$NPV_A(r_1) = NPV_B(r_1): \rightarrow r_1 = 5.2\%$$

$$NPV_B = -100 + \frac{115}{1+r} \text{ and } NPV_A = -100 + \frac{121}{(1+r)^2}$$

2.3 Annual User Charge (AUC)

Concepts:

Opportunity Cost:

The opportunity cost of a project is what is forgone by undertaking the project — i.e. the value of resources in next best use.

Depreciation (economic):

The change (fall) in market value of an asset.

Implicit rental cost:

The opportunity cost of holding (owning) an asset. (e.g. a machine)

- = the implicit rental cost
- = the sum of:

the interest forgone on outlay + depreciation + any operating costs.

(Don't use straight line depreciation: use annuity.)

Example of Annual User Charge:

Purchase of vehicle.

Bought for \$2
Sold at \$1 one year later. i = 10% p.a.; costs \$0.30 to run for one year
Interest charge = $$2 \times 0.1 =$ $0 = $2 \times 0.1 =$ 0 = \$1.00Operating cost = 0.30 0.30 0.30 0.30

Marginal cost:

How much more does it cost to produce an extra unit of output?

Average cost:

What does it cost per unit of output?

2.4 Net Present Value

[DoF Ch. 4; L. 2.3; FP Ch. 5.1]

Calculate NPV (or NPB) of each project using r_m (the *appropriate* market rate or rates—they may vary through time—of return) (Using the formula on Lecture 3 2, above.)

> 0 then the project is OK

if NPV = 0 indifferent

< 0 then the project is not OK, because the return ("the appropriate market rate") is higher than the return from this project.</p>
The opportunity value is negative.

If there are many projects, mutually exclusive, and there is no budget constraint,

then rank by *positive* NPV > 0 and go with the largest NPV, since this project maximises the size of the return.

Yes, if only 1 chosen.

No, if can choose several.

Three types of decision:

1. accept or reject accept if NPV > 0

reject if NPV < 0

2. ranking

- (a) If no capital budgeting, (or other rationing), then accept all projects with NPV > 0
- (b) If there is *capital budgeting,* (See 2.13., below) then rank: by B/C, not by NPV

2.4.1 Value On Completion

A project involves:

- cash investment outlays $-x_t$ without receipts over the first T years of the project,
- followed by net operating revenues x_t over the operating life of the project represented by L.

The NPV of the project can be assessed as:

$$NPV_0 = -X_0 - \frac{X_1}{1+r} - \frac{X_2}{(1+r)^2} - \dots - \frac{X_T}{(1+r)^T} + \frac{X_{T+1}}{(1+r)^{T+1}} + \dots + \frac{X_{T+L}}{(1+r)^{T+L}}$$

An equivalent but simpler method is to compute the *Value On Completion* (VOC):

$$VOC_T = x_0(1+r)^T + x_1(1+r)^{T-1} + \cdots + x_T$$

That is: accumulate forward your investment outlays at the cost of capital, to the last date (T) at which the completed project costs.

VOC Criterion.

Then: Compare VOC_T with NPV_T , where both evaluations refer to the same date.

So we compute:

$$NPV_T = \frac{X_{T+1}}{1+r} + \frac{X_{T+2}}{(1+r)^2} + \cdots + \frac{X_{T+L}}{(1+r)^L}$$

Note:

$$NPV_0 = \frac{NPV_T - VOC_T}{(1+r)^T} > 0$$
 if $NPV_T > VOC_T$

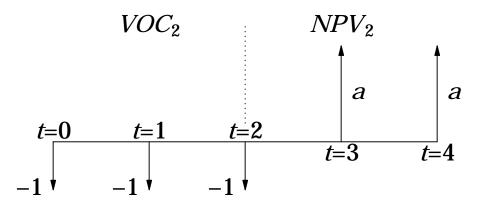
Criterion: Accept the project if the VOC is less than or equal to the NPV of cash flows over the operating life of the project.

Moreover,

VOC = Direct Capital Outlays + Interest During Construction

Example 1 of VOC:

\$1 is outlaid at the beginning of each of 3 periods (T=2). The asset operates for two years, yielding a net revenue stream of a (L=2). The discount rate r=10% p.a.



$$NPV_{0} = -1 - \frac{1}{(1.1)} - \frac{1}{(1.1)^{2}} + \frac{a}{(1.1)^{3}} + \frac{a}{(1.1)^{4}}$$

$$VOC_{T=2} = (1.1)^{2} + 1.1 + 1 = 1.21 + 1.1 + 1 = 3.310$$

$$NPV_{T=2} = \frac{a}{1.1} + \frac{a}{(1.1)^{2}} = \frac{2.1a}{(1.1)^{2}} = 1.736a$$

$$VOC_{T} < NPV_{T}?$$

Accept if 3.310 < 1.736a, or if a > 1.9072.

The annuity equivalent of $VOC_{T=2} = 3.310$ is A = 1.9072. Hence the net revenue must exceed A i.e., a > A.

Example 2 of the "VOC" Approach

The (early '90s) Very Fast Train (VFT):

Investment Outlay: \$900m p.a. for each of 5 years

Cost of capital (assume 9.06% p.a.) (CRIF database) (CRIF = AGSM's Centre for Research in Finance.)

Direct capital cost = \$4.5 billion

Value On Completion = \$5.393 billion (includes return on capital)

∴ Annual User Charge = \$591 m p.a. (20 yr life)

(\$5.393 bn is the value of an annuity of \$591 m over 20 years.)

Operating and maintenance costs = \$218m p.a.

∴ Total annual costs = \$591 + \$218 million = \$809 million

Equivalent to 6¼ million passengers each paying \$129 per trip.

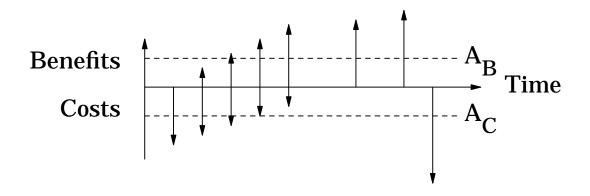
NPV when first dollar is outlaid is zero.

(So VOC equivalent to NPV (when costs & benefits are discounted to T=0). Instead, the VOC takes costs & benefits to a date after investment is begun.)

2.4.2 Annual Value (Equivalent Annuities) [DoF pp.46]

 $GPB \rightarrow equivalent annuity A_B: PV(A_B) = GPB$

 $GPC \rightarrow A_C$: $PV(A_C) = GPC$



But AV: NPV

$$\operatorname{GPC} o A_C$$
 $\operatorname{GPB} o A_B$ rank by $(A_B - A_C)$ ~ NPV

2.4.3 Annuities and All That

[Bishop, Crapp, Faff, and Twite Ch 4]

$$FV = F_n = F_0(1+r)^n$$

$$FV = F_n = F \frac{(1+r)^t - 1}{r}$$

where FV is the *future value* of an amount F_0 and r is the discount rate over n periods; where F is an *annuity* of over t periods.

When n is infinite, we have a *perpetuity*. In present value terms:

$$PV = \frac{F_n}{(1+r)^n}$$

$$PV = F \frac{1 - (1+r)^{-t}}{r} \quad \text{annuity}$$

$$PV = \frac{F}{r} \quad \text{perpetuity}$$

$$\therefore F = \frac{PV}{\frac{1 - (1+r)^{-t}}{r}}$$

2.5 Internal Rate of Return

[DoF pp.114; L. 2.4; FP,Ch.5.2]

IRR is the interest rate which makes the *NPV* of the project zero.

Example: a cost of \$1 now, a return of \$1.10 in one period.

$$NPV = -1 + \frac{1 \cdot 1}{1 + i} = 0$$

 \therefore Internal rate of return = 10% = i

In general,
$$NPV = \sum_{t} \frac{X_t}{(1+i^*)^t} = 0 \rightarrow i^* = IRR.$$

Rule: undertake the project if its internal rate IRR exceeds the external yield (the market interest rate)

Note: if projects are *mutually exclusive*, we cannot rank them by their internal rates of return.

IRR solves for the rate r which makes the present value of net benefits equal zero, or $GPB(r^*) = GPC(r^*)$.

IRR =
$$r^*$$
: $\sum_{t=0}^{T} \frac{b_t}{(1+r^*)^t} = \sum_{t=0}^{T} \frac{c_t}{(1+r^*)^t}$, (where c_0 includes K_0)

IRR compared to Market Rate

We compare the IRR with r_m , the appropriate market rate:

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if IRR > r_m then OK on opportunity cost grounds
if IRR < r_m then not OK
if IRR = r_m indifferent
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If there exist many mutually exclusive projects, then rank in terms of their IRRs and go with the highest?

No.

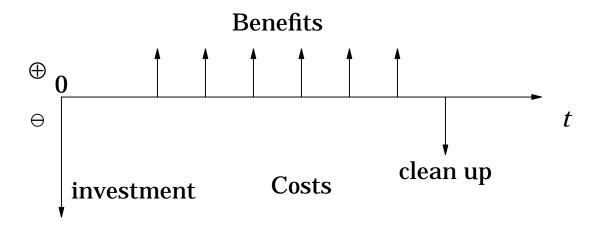
But there are problems with IRR. (See Luenberger in the Package.)

Criticisms of IRR:

- 1. Lack of uniqueness (may be several IRRs, r^*).
- 2. Different time profiles of costs and benefits may result in ambiguous ranking.

Problems with IRR [L. 2.5]

NB: Neither IRR nor B/C can be adequately used to choose between two mutually exclusive projects.



(a common profile)

$$\Rightarrow$$
 IRR = 4%, 17%



Sign check: when $r = \infty$, NPV < 0

.. no unique IRR if NPV behaves as shown.

2.6 Benefit/Cost Ratio

[DoF pp. 112; FP Ch. 5.5]

Calculate the ratio of $\frac{\text{p. v. of benefits}}{\text{p. v. of costs}} = \frac{B}{C}$ or

$$\frac{\sum_{t=0}^{T} \frac{b_t}{(1+r_m)^t}}{\sum_{t=0}^{T} \frac{c_t}{(1+r_m)^t} + K} = \frac{B}{C}$$

If $\frac{B}{C} > 1$, then the project is OK, according to this criterion. \Leftrightarrow NPV \equiv B - C > 0.

Mutual Exclusivity

If there are many mutually exclusive projects, then rank in terms of $\frac{B}{C}$ ratio and choose the project with the largest ratio?" No — it's scale independent. This doesn't guarantee that NPV is maximised, and so the best project chosen. There is, however, a rôle for B/C when there is *capital rationing*. (See 2.13. below.)

Net Benefit Investment Ratio, NBIR

$$NBIR = \frac{\sum_{t=0}^{T} \frac{B_t - OC_t}{(1+i)^t}}{\sum_{t=0}^{T} \frac{IC_t}{(1+i)^t}}$$

where OC_t are the project's operating costs in period t, IC_t are the project's investment costs in period t, B_t are the benefits in period t, i is the appropriate discount rate.

Separates the project's operating costs and investment costs, to enable calculation of the net operating profit per present value dollar invested.

2.7 Payback Period

[DoF pp. 115; FP Ch. 4.10.2]

$$\frac{K}{b_t}$$
, implicitly $r = 0$

- not necessarily consistent with NPV
- bias towards projects with front end returns (i.e., if recover costs in $t \le \tau$ then O.K.)

2.8 Inflation

[DoF pp. 52; L. 2.6; FP Ch.4.9]

(Inflation: An increase in the general price level)

NPV is invariant to the inflation rate!

Let R = nominal interest rate

i = real interest rate

g = rate of inflation of all prices

$$1 + R = (1 + i)(1 + g) = 1 + ig + i + g$$

$$\therefore R \approx i + g$$
, or $i \approx R - g$.

looking ahead: inflation rate?

1. In NPV analysis we can project price increases into the future and use nominal interest rate, R. (dollars of the day)

or

- 2. Can forget about future general price increases and use real interest rate *i*. (adjusted for inflation)
- 3. We get the same answer in both cases.

Example with Inflation:

Cost of \$1 now, a real return of \$1.10 in one period; nominal return $\approx 1.10 \times (1+g)$.

$$NPV \approx -1 + 1.1 \frac{1+g}{1+R}$$
 (nominal)
= -1 + 1.1 \frac{(1+g)}{(1+i)(1+g)}
= -1 + \frac{1.1}{1+i} \text{ (real)}

If i = 10%p.a., NPV = 0 regardless of inflation rate g.

... NPV is *not* a function of the inflation rate!

2.9 Income Tax

[FP Ch. 3.6]

If capital income and interest receipts are taxed at rates τ_c and τ_i respectively (with payments deductible), then:

- pre tax interest rate = i
- post tax interest rate = $i(1 \tau_i)$
- *i* is used to discount pre tax cash flows
- $i(1-\tau_i)$ to discount after tax cash flows

Example with Taxes:

Taxi Plate

Net cash flow
$$i$$
 = \$10,000 p.a. pre tax i = 10% p.a. $\tau_c = \tau_i$ = 50%

NPV (pre tax) = $\frac{\$10,000}{0.1}$ = \$100,000 for a perpetuity

NPV (post tax) = $\frac{\$10,000(1-\tau_c)}{0.1(1-\tau_i)}$ = $\frac{\$10,000(1-0.5)}{0.1(1-0.5)}$ = \$100,000 (perpetuity)

What if the two tax rates are not equal?

2.9.1 Classical tax system versus Imputation system

Suppose: Nominal interest rate R = 15% p.a. Expected inflation rate g = 10% p.a. \therefore Real interest rate $i \approx 5\%$ p.a. Risk premium on equity = 7% p.a. Corporate tax rate (nominal effective) = 39% = 50.50

Classical (pre 1987) cost of capital:

Pre tax (nominal) basis: ½ debt + ½ equity

$$15\%(0.5) + \frac{15\% + 7\%}{1 - 39\%}(0.5)$$
= 25.5% nominal

since the required 22% nominal return on equity is grossed up by the corporate tax factor (1 - 39%).

Pre tax (real) basis: 25.5% - 10% = 15.5% real

With the tax imputation system for dividends (post 1987),

company tax at the rate of 39% is effectively abolished for Australian taxpaying owners of Australian companies, so that the weighted average discount rate (nominal) is:

$$15\%(0.5) + (15\% + 7\%) (0.5) = 18.5\%$$
 nominal $\rightarrow 8.5\%$ real (for such a personal investor.)

2.10 Discount Rates for Private (and Public) Sector Projects:

Four concepts:

- 1. Social Rate of Time Preference (SRTP) people's valuation of the future (consumption)
- 2. Social Opportunity Cost of Capital (SOCC) competing investments
- 3. Project specific use Capital Asset Pricing Model $\rightarrow \beta$ for the project
- 4. Cost of Funds
 debt borrowing
 equity owning
 (See the example in 2.9.1 on Tax.)
- 5. Special Cases

2.10.1 Social Rate of Time Preference

Society's preference for present consumption versus future consumption.

or: the additional future consumption required to exactly compensate for postponement of a unit of present consumption.

SRTP ≠ individual's RTP necessarily

Estimate of SRTP:

The exchange of government bonds \rightarrow bond rate

- long term (up to 50 years)
- certain nominal costs and returns:
 say, buy at \$100, receive \$110 after a year
- small units
- available to all

At the margin, the return is equal to all (MRS), say, 10% p.a. nominal (or lower?)

Adjust for inflation: 10 - 3 = 7% p.a. (real) Adjust for taxation: $7(1 - \frac{1}{3}) = 4.7\%$ p.a.

But: some seek higher returns, while some invest nothing.

Net: is SRTP an upper bound?

2.10.2 Social Opportunity Cost of Capital

The return on the investment that is displaced by the marginal project.

With fully competitive markets: SOCC ~ SRTP

With tax etc.: SOCC > SRTP

Net benefits are consumption, not investment.

Estimate: bond rate of 10% p.a. nominal, before tax + risk premium 2%

 \therefore real = 12% – expected inflation of 3%

∴ real = 9%

tax adjustment of $9(1 - \frac{1}{3}) = 6\%$ effective

2.10.3 Project Specific Rates

Use CAPM to get market premium (2.1 7.9%) (Use AGSM Centre for Research In Finance (CRIF) database.)

2.10.4 Cost of Funds

If the government is borrowing, then the long term bond rate. If private borrowing, see examples in 2.9.1 on Tax.

A Bias Towards Government Projects?

If we use the lower SRTP, then

- government projects face a lower hurdle, while
- private projects (SOCC or higher) face a higher hurdle.
 - ∴ a bias towards government projects
 - → infrastructure bonds (lower discount rate) for private projects in order to lower the private cost
 - → SOCC or project specific rates for the government

DoF: 8% p.a. as benchmark (real) = 2% margin + 6% risk free (Probably too high for a risk free rate now, 2003.)

SRTP versus SOCC

	<i>Time preference</i> SRTP	<i>Opportunity cost</i> SOCC
Goal	Achieve a preferred flow of net benefits over time.	Increase net income to society.
Time span	Long term—as long as individuals plan (say, one to two generations)	Short term—as long as the life of displaced private investment (say, up to 15 years)
Estimation can start from	government bonds	government bonds plus a risk premium
"Typical" real rates, after adjustment for taxation	4% to 7%	Above 7%

(from Sinden & Thampapillai, p.134)

2.11 Consistency of Horizon Choice

[L p. 25,26,29]

The plantation costs \$1 to establish.

Two choices:

- cut it down after one year to receive \$2, or
- wait until the end of the second year and reap \$3.

Net Present Value @ 10% p.a.:

- A. NPV of cutting sooner is $\$0.82 = -1 + \frac{2}{1.1}$ B. NPV of cutting later is $\$1.48 = -1 + \frac{3}{1.1^2}$

So (B) *later* looks more attractive.

Internal Rate of Return (irr):

- A. Solve -1 + 2c = 0 where $c = \frac{1}{1 + irr}$, then irr = 1.0 or 100%.
- B. Solve $-1 + 3c^2 = 0$, so $irr = \sqrt{3} 1 = 0.7$ or 70%.

So (A) *earlier* looks more attractive.

But the time horizon isn't OK:

A takes only 1 year, versus 2 years for B.

If we repeat (A) twice, its NPV is given by

NPV(A twice) =
$$0.82 (1 + \frac{1}{1.1}) = 1.5654 > 1.48$$

So choose (A = earlier) repeated.

The IRR of twice A is unchanged: 100% per year for both years.

Or: Solve
$$-1 + 2c + c(-1 + 2c) = 0$$
, gives $c = -1$ or $\frac{1}{2}$, gives $irr = 1.0$ or 100% , (ignoring the negative root for c).

Another reason:

if the projects are repeated and the principal is reinvested, then (A) leads to doubling of principal every year, whereas (B) only grows at $\sqrt{3}$ = 1.73 every year.

Note that the growth rate with reinvestment of principal = 1 + *irr* always.

2.12 Non Mutually Exclusive Projects.

Project	GPC	GPB	∴NPV	$\frac{GPB}{GPC}$	NPV	B/C
X Y Z Z'	100 50 50 55	200 110 120 130	100 60 70 75	2.0 2.2 2.4 2.36	① ③ ②	3 2 1
Y+Z new: Y+Z'	100 105	230 240	130 135	2.3 2.29		
status quo	50	50	0			

Ranking by NPV \rightarrow X, Z, Y

Ranking by B/C \rightarrow Z, Y, X

Ranking $\{X,Y,Z'\}$ by $B/C \rightarrow Z'$, Y, X

If capital budget = 100, and all costs immediate:

then rank by B/C & use up budget, but take care: $\{Z',Y,X\}$: can't choose Y, Z' > 100

but if choose Y alone, NPV = 60

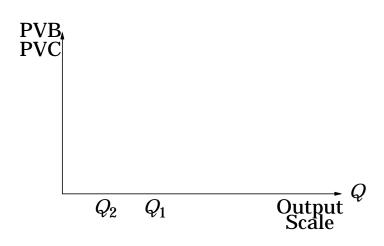
Non separability:

— what if there is jointness in costs?say, Y+Z costs only 95 instead of 100.

— what if there are side effects on discount rates?

Comparing max NPV and max B/C.

	PV Costs	PV Benefits	B/C	$ NPV \\ = PVB - PVC $
Project XX	200	450	2.25:1	250
Project YY	400	800	2.00:1	400
Project ZZ	600	900	1.50:1	300



(identical except for scale)

at Q_1 : MB = MC \rightarrow max NPV \equiv B-C

at Q_2 : max B/C

e.g.

2.13 Capital Rationing

[FP Ch. 5 App. 1; S&W, Ch. 6.2]

Aim of agency or firm: to maximise its financial surplus, subject to its capital budget.

e.g.A public agency may spend up to \$1.8m in year 0. Four independent, *divisible* (which means that fractional (≤ 1) projects are possible) projects are under consideration:

Project	Cost in year 0	Net returns	Life of project	Gross
-	(to be paid from	per year:	(number of years in	Present
	capital ration)	year 1 onwards	which net returns	Benefit
	\$m	\$m	occur)	
A	1.0	0.14	20	1.19
В	1.0	0.13	50	1.29
C	2.0	1.00	3	2.49
D	1.0	0.25	8	1.33

Capital Rationing

Choose projects with the highest present value of capital used. At r = 10% pa, the NPVs are calculated:

Project	NPV of project in year 0	Present value per unit of capital	Internal rate of return
	\$m	\$	(%)
A	0.19	0.19	13
В	0.29	0.29	13
C	0.49	0.24	23
D	0.33	0.33	19
		= NPV/K	_
		= NPV/GPC	

The most efficient investment is \$1.0m in Project D and the remaining \$0.8m in Project B. This produces a total NPV of $0.56m (= 0.33 + 0.8 \times 0.29)$.

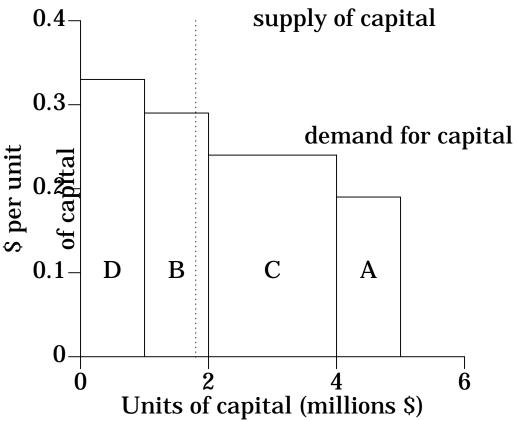
= (B-C)/C

If another \$1 is available for investment, then we should invest further in Project B, increasing the NPV of the agency's financial surplus by \$0.29. So one unit of capital, of a nominal value of \$1, has at the margin a value of \$1.29 with capital rationing.

The marginal opportunity cost of capital is \$1.29. We refer to this as a **shadow price** (greater than the nominal price of \$1 because of the capital constraint).

Capital Rationing — Diagram

We can interpret this constraint with a simple supply–demand for capital figure: [S&W, Fig. 6.1]



Areas = **NPV** of **projects**.

2.14 Summary

[DoF p.54]

- Cost and benefits occurring at different times have different values. The
 present value of that stream of costs or benefits is the value in today's
 dollars, calculated using the method of compound interest, with the
 discount rate as the exchange rate between future dollars and today's
 dollars.
- Subject to budget constraints, and where alternative projects are not under consideration, a project should be accepted if the sum of its discounted benefits exceeds the sum of its discounted costs; that is, where its *net present value (NPV) is positive*.
- Where *alternative projects* are under consideration, the project which maximises NPV should be selected.
- Where *budget constraints* limit the number of projects which can be undertaken, the appropriate decision rule involves choosing that subset of the available projects which maximises total NPV.

• Provided that future budget constraints can be forecast, it is possible to work out the *optimum timing* of projects; sometimes the combined NPV will be greater if projects with "lower" NPVs are undertaken first.

- Other decision rules, such as the *benefit/cost ratio* and the *internal rate of return* (IRR) may be included in the analysis alongside the NPV criterion, but, since these rules can be misleading except in restricted circumstances, they should not be used instead of the NPV criterion.
- When it is expected that projects of *short lives* will lead to further projects which yield above normal returns, it is necessary to adjust the alternative investments so that they span about the same period of time.
- Evaluations should normally be undertaken in *real values* that is, the price level of a given year but this assumes that future inflation will affect all costs and benefits equally. Where this is incorrect, cash flows should be separately adjusted for inflation, and the assumptions regarding relative price changes made explicit.
- Do not confuse *real and nominal prices and discount rates* in the same analysis: where the analysis is in terms of nominal prices, the discount rate must be adjusted up to account for the expected inflation rate.

Alternative Decision Rules [DoF pp.117]

• The IRR will only provide a correct result when *all* of the following conditions apply:

- no budget constraints
- 2. project alternatives are not mutually exclusive
- 3. the net benefit stream is first negative, and then positive for the remainder of the project's life (or vice versa).
- Similarly the benefit cost ratio is only as reliable as the NPV rule when there are no budget constraints and project alternatives are not mutually exclusive.
- While the discounted payback period (PBP) rule is superior to the undiscounted PBP rule, and while analysts may learn to select a cut off which reduces the risk of bad choices, the PBP rules are not as reliable as the NPV rules, and so should be avoided.
- Conclusion:

The NPV rule should be the primary basis for decision making, and should *always* be included.

Discount Rates [DoF pp.57]

- Two main concepts of the discount rate:
 - 1. the social rate of time preference (SRTP), corresponding to society's preference for present as against future consumption; and
 - 2. the social opportunity cost of capital (SOCC), corresponding to the rate of return on investment elsewhere in the economy.

Generally the SRTP is lower than the SOCC.

- A project specific discount rate can be determined from the SOCC, using the CAPM framework.
- A fourth measure uses the direct or observed cost of funds the cost of borrowing for a government.
- The SOCC is preferred, to reduce the risk that public investment displaces higher yielding private investment.
- A CAPM approach is preferred, but not always feasible.

Summary of Week 2

These lectures discussed

Q: How to decide? Which criterion is the best?

A: In general, NPV and its derivatives (AUC, VOC, Annual Value, Annuities).

- The weaknesses of Internal Rate of Return.
- Problems with the Benefit/Cost ratio, but
- its use when there is capital rationing in order to maximise net value added across projects.
- Problems with the Payback method.
- Inflation issues use either real (inflation adjusted) or nominal, but don't mix them.
- Income tax issues.
- Which discount rate to use? Social discount rate, or Social opportunity cost of capital?
- Make sure that time horizons are comparable across projects.