Question 1

The graph below plots the natural log of the monthly closing prices of the SP500 index from March 1980 to June 1999. The graph is plotted such that March 1980 corresponds to time, $T=0$, April 1980 $T=1$, …, June 1999 $T=231$. 
(i) What type of relationship describes the growth of the SP500 index over time?

(ii) What is the average *monthly* growth rate expressed continuously?

(iii) What is the average *annual* growth rate expressed continuously?

(iv) What was the value of the SP500 index at March 1980 (i.e. when T=0)?

(v) Let S be the value of the SP index. Express S as a function of time in months?
**Question 2**

The graphs below depict the number of car fatalities in a state as a function of that state’s population (state population is given in 1000’s).

The line of best fit for the data in the right panel is 

\[ y = -1.0 + 2x/3 \]

(i) What type of function best describes the relationship between the number of fatalities in a state and the population of that state?

(ii) Write down an expression for the number of fatalities as a function of population.

(iii) If you were told that a state’s population was 15,000 (expressed in thousands) what would be your best guess of that state’s car fatalities?
Question 3

A researcher decided to examine the effect of the length of time MBA students spent studying on the performance of these students on a maths exam. Students were given material that they had never seen before and examined on this material one week later. The data is summarized in the graph below.

![Graph showing the relationship between % Grade on Exam and Hours Studying. The relationship looks non-linear.](image)

The relationship looks non-linear and to determine the nature of the relationship between “% Grade on Exam” and “Hours Spent Studying” the researcher decides to construct the following two plots. The first graph plots the “ln(%) Grade on final exam”) vs “Hours Spent Studying”. The second graph plots “ln(%) Grade on Exam)” vs “ln(Hours spent studying)”
(i) On the basis on these graphs what type of function best describes the relationship between “% Grade on Exam” and “Hours spent studying? Explain

(ii) Given your answer to part (a) write down the function that relates “% Grade on Exam” to “Hours spent studying”

(iii) If a student spends 3 hours studying what grade would that student expect.

(iv) If a student spends 20 hours studying what grade would that student expect.
Question 4

Microsoft shares were trading for $1.21 at the end of December in 1989. The annual growth rate of Microsoft shares for the 1990’s was 57.9%, expressed as ordinary compound interest.

(i) What was the annual growth rate expressed as a continuous compound rate?

(ii) What was the monthly growth rate expressed continuously?

(iii) If the natural log of monthly prices of Microsoft for the 1990’s were plotted against time (measured in months) we would observe a straight line. What would be the intercept of this line?

(iv) What would be the slope?

(v) Let Y be the natural log of the monthly closing price of Microsoft shares. Express Y as a function of time.

(vi) Let S be the monthly closing price of Microsoft shares. Express S as a function of time.
**Question 5**

Data were collected on the demand of used refrigerators versus the price charged and are plotted below.

![Price vs Demand Used Refrigerators](image)

You decide to construct the following graphs in order to determine the relationship between Demand and Price.

![Price vs Ln(Demand)](image)
(i) What type of relationship best describes the relationship between Demand and Price?

(ii) Write down the relationship between Demand (Q), and Price (P)?
Question 6

The graph below plots the natural log of daily closing prices of the All Ords Index from April 2003 to Oct 2003. The graph is plotted such that April 1\textsuperscript{st} 2003 corresponds to time, T=0, April 2\textsuperscript{nd} 2003 T=1 etc.

(i) What is the average \textit{daily} growth rate expressed \textit{continuously}?

(ii) What is the average \textit{annual} growth rate expressed as \textit{continuously} compound interest?

(iii) What is the average \textit{annual} growth rate expressed as an \textit{ordinary} compound rate?

(iv) What was the value of the All Ords Index in April 1\textsuperscript{st} 2003 (i.e. when T=0)?

(v) Write down an expression for the value of the All Ords index as a function of time?